

Common fixed point results in b-cone metric spaces over topological vector spaces ¹

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Abstract

In this paper we introduce the notion of b-cone metric space over topological vector space (for short *b-TVS cone metric space*) and prove some common fixed point theorems in complete b-cone metric spaces over topological vector spaces. These results generalize, extend and unify several well-known recent related results in literature.

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